Mg/(Mg+Fe)	Dhaaa	-		Vp	Vs	$V_{\rm S}$	K	$\left(\frac{\partial K_{s}}{\partial K_{s}}\right)$	Remarks
mole %	Phase	m	ρ (g/cm ³)	(km/sec)		(Mb)	$\left(\frac{1}{q_{6}}\right)$	Remarks	
100	Olivine	20.1	3.217	8.534	4.977	6.309	1.281	5.04	Experimental
	Spinel	20.1	3.556	9.66	5.54	7.24	1.86	4.4	Estimated
95	Olivine	20.6	3.273	8.422	4.892	6.245	1.277	5.08	Experimental
	Spinel	20.6	3.620	9.57	5.48	7.18	1.87	4.4	Estimated
90	Olivine	21.0	3.330	8.317	4.815	6.189	1.274	5.13	Experimental
	Spinel	21.0	3.683	9.49	5.42	7.13	1.87	4.5	Estimated
85	Olivine	21.5	3.386	8.216	4.739	6.132	1.272	5.13	Experimental
	Spinel	21.5	3.750	9.41	5.36	7.10	1.88	4.5	Estimated
80	Olivine	21.9	3.440	8.116	4.663	6.075	1.269	5.23	Experimental
	Spinel	21.9	3.815	9.33	5.29	7.05	1.89	4.6	Estimated
50	Olivine	24.6	3.800	7.534	4.213	5.753	1.258	5.44	Experimental
	Spinel	24.6	4.209	8.85	4.92	6.78	1.93	4.8	Estimated
0	Olivine	29.1	4.393	6.637	3.494	5.273	1.220	5.92	Experimental
	Spinel	29.1	4.849	8.05	4.28	6.35	1.96	5.1	Estimated
			±0.2%	±0.5%	±0.5%	±0.8%	±1.8%	±5.0%	Expected error

	Table 1	
Elastic properties of olivine and	olivine-transformed spinels in the Mg_2SiO_4 -Fe ₂ SiO ₄ system *.	

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* Data from ref. [3].

D.H. Chung, Olivine-transformed spinels

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D.H. Chung, Olivine-transformed spinels

Birch's law for the bulk sound velocity-density-mean atomic weight relation is

$$V_{\phi} = a + b\rho \tag{2}$$

where the constants a and b can be obtained from a least squares fit of experimental values of V_{ϕ} obtained from substances of similar mean atomic weight (or from substances of the same mean atomic weight, as was done by Wang [8]). In terms of Birch's law, Chung [13] has shown that

$$\left(\frac{\partial K_{\rm s}}{\partial p}\right)_{\rm s,\bar{m}} = \mathbf{I} + \frac{2 b \rho}{V_{\phi}} + \frac{\mathbf{C}}{K_{\rm s}}$$
(3)

where K_s is in megabars and V_{ϕ} is in kilometers per second. Using eq. (3), values of $(\partial K_s/\partial p)$ for the olivine-transformed spinels were calculated from ρ , V_{ϕ} , and K_s in table 1; in table 2, these calculated results are then compared with earlier estimates made by this author. The agreement between these two sets is satisfactory.

Although the chemistry of spinels in the (Mg,Fe)Al₂O₄ compositions differs from that of the $(Mg,Fe)_2$ SiO₄-spinels, their elastic properties are probably identical.* Support for the present estimates of equation-of-state parameters for the olivine-transformed spinels then comes from recent ultrasonic measurements of $(\partial K_c/\partial p)$ for spinels in the (Mg,Fe) Al₂O₄ system. The elastic constants of the stoichiometric $MgAl_2O_4$ spinel were first studied by Chung et al. [15] with hot-pressed polycrystalline samples. Lewis [16] and more recently O'Connell and Graham [17] studied the single-crystal elastic properties of this spinel; their results at ambient conditions are found to be in good agreement with the results from polycrystalline work. Schreiber [18] measured a $(\partial K_s/\partial p)_T$ value of 4.18 for a spinel with the Mg(2.6) Al_2O_4 composition. Chung [32], working with polycrystalline stoichiometric MgAl₂O₄ spinel, determined a $(\partial K_c/\partial p)_T$ value of 4.3 (±0.25). Using spinel of the same composition, but working with single crystals, O'Connell and Graham [17] found the value of 3.76. O'Connell and Graham [17] also measured $(\partial K_s/\partial p)_T = 3.76$ for the same specimen of Mg(2.6) Al₂O₄ spinel that Schreiber [18] used in his original work; thus the apparent disagreement is noted for the work of refs. [17] and [18]. (The apparent difference in the $(\partial K_c/\partial p)_T$ value measured on the same sample, but different investigators, seems to represent the present state-of-the-art in the attempt to characterize this important equationof-state parameter of mantle minerals). In their recent paper, Wang and Simmons [19] reported a $(\partial K_s/\partial p)$ value of 4.9 (±0.25) for a pleonaste-spinel of the "(Mg_{0.75}Fe_{0.36}) Al_{1.9}O₄ composition". For comparison with the elastic parameters estimated for spinels in the $(Mg_xFe_{1-x})_2SiO_4$ system, the density and other parameters of various spinels in the (Mg,Fe) Al₂O₄ compositions are listed in table 3. As is clearly shown in table 2 and 3, the elastic properties of these spinel compositions are similar; values of K_{e} are in the neighborhood of 2 Mb and for $(\partial K_s/\partial p)$ values are about 4 to 5. Thus, in the absence of experimental measurement, the equation-of-state parameters of the $(Mg_rFe_{1-r})_2SiO_4$ -spinels estimated in this report provide a basis for specifying the desired equations of state of these olivine-transformed spinels in the Mg_2SiO_4 -Fe_2SiO_4 system.

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^{*} From the structural point of view, the spinels in the (Mg, Fe) Al_2O_4 system differ in two ways from those of the (Mg, Fe) $_{2}SiO_{4}$ composition. In the former case, there are 8 (Mg, Fe) Al_2O_4 units per unit cell, wherein the divalent cations are in the fourfold coordination and two trivalent aluminum ions are in the six fold coordination. In the latter case, there are 8 (Mg, Fe) ,SiO₄ units per unit cell; the divalent cations, which are twice as numerous as the tetravalent silicon in a given unit cell, are in the fourfold coordination and the silicon ion in the sixfold coordination. In both cases, however, the structure consists of a cubic closely-packed array of oxigen ions with the sixfold coordinated cations occupying the octahedral interstices and the divalent cations the tetrahedral interstices. Ionic sizes of these cations in the octahedral sites do not differ much, i.e., according to Pauling [14] Al³⁺ has the ionic radius of 0.50Å and Si⁴⁺ has 0.41Å. One would expect that, for the same (Fe/Mg) ratio in the tetrahedral sites in these two spinel compositions, the elastic properties like the bulk modules and its rate of change with pressure would not differ very much from each other. However, because there are twice the number of iron atoms in the (mg,Fe) 2SiO4 composition as compared with the (Mg, Fe) Al₂O₄ spinels, the greater effect of an iron sustitution for magnesium on the elastic properties would be expected for the (Mg,Fe)₂SiO₄ composition than for the Al₂O₄ spinels.